

Four Boosted Tops from a Regge Gluon

arXiv:0907.3496, 1106.2171

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Outline

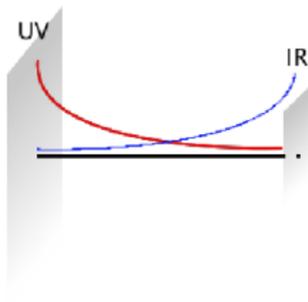
- 1 Introduction & Background
 - Randall-Sundrum Models
 - String Theory
- 2 The Warped Space Regge Gluon
 - Kaluza-Klein Expansion
 - Interactions with Standard Model
- 3 LHC Phenomenology
 - Decays of the Regge Gluon
 - Signals and Backgrounds

Randall-Sundrum Models

Background, Notation and Conventions

Randall-Sundrum models have 5D warped geometry:

$$ds^2 = \exp(-2k|y|) dx^\mu dx_\mu - dy^2; \quad y \in [0, L].$$



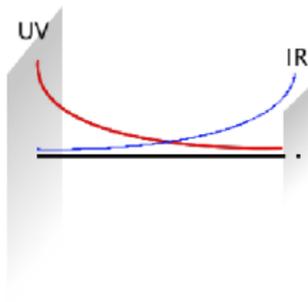
- Relevant Scales:
 $k \sim \text{Planck}$; $kL \sim 35$;
 $\Lambda \equiv k \exp(-kL) \sim \text{TeV}$.
- Higgs localised at $y = L$ (IR);
Natural mass scale Λ .
- Other SM fields propagate in bulk;
- KK scale \sim a few times Λ .
- Warping \Rightarrow light stringy effects?

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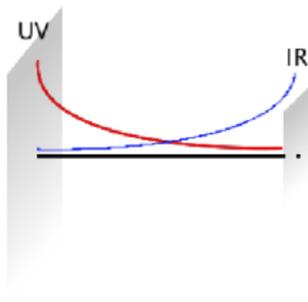
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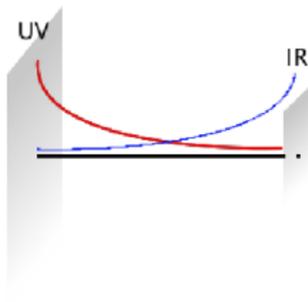
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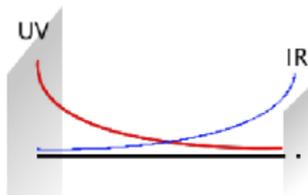
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String Theory in General and in RS

Regge States and Veneziano Amplitudes

We (I?) can't do String Theory in RS.

- Warped backgrounds not under theoretical control

High Spin (Regge) States!

- Characteristic of stringy physics
- Bosonic string: n th harmonic:

$$M_n^2 = \frac{1}{\alpha'} n^2$$

- Veneziano amplitudes:

$$\mathcal{A} \propto \frac{\Gamma(1-\alpha's)\Gamma(1-\alpha't)}{\Gamma(1-\alpha's-\alpha't)}$$

- Regge poles at $s = n M_s^2$

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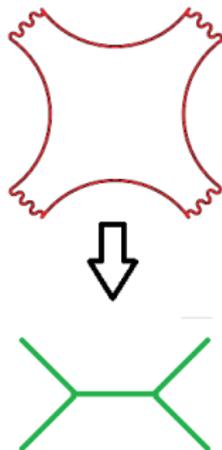
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An Effective Field Theory Perspective

Model-Building Philosophy



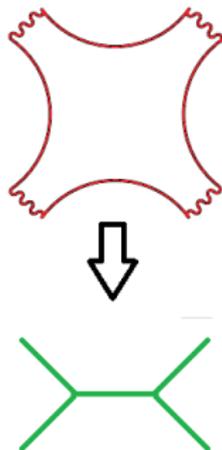
- 1 Take toy string model of QCD in flat space
- 2 Compute scattering amplitudes \mathcal{A}
- 3 Factorise on first Regge pole
- 4 Construct **EFT** that reproduces stringy \mathcal{A}
 - (Focus on spin 2 gluon partner)
- 5 **Covariantly generalise** theory to RS
- 6 Integrate over extra dimension
 - (KK expansion)

Warning! Not a well-defined approximation to string theory!

See Rosa et al, 0904.4108 for spin-3/2 top partner

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Spin-Two Quadratic Terms

Free tensor action in RS:

$$\begin{aligned} \mathcal{L}_2 = & \frac{1}{4} H_{LMN} H^{LMN} - \frac{1}{2} H_{LM}{}^M H^{LN}{}_N \\ & + \frac{1}{2} (3k^2 + m^2) ((B_M{}^M)^2 - B_{MN} B^{MN}) \\ & - k [\delta(y) - \delta(y - L)] ((B_\mu{}^\mu)^2 - B_{\mu\nu} B^{\mu\nu}). \end{aligned}$$

- M (μ) 5D (4D) coordinates
- Field Strength Tensor $H_{LMN} \equiv \nabla_L B_{MN} - \nabla_M B_{LN}$
- Terms involving k are kinetic, from curvature tensors
- Gauge symmetry: $\delta B_{MN} = \nabla_M \beta_N + \nabla_N \beta_M$
- Implied boundary conditions:

$$(\partial_y \pm 2k) B_{\mu\nu} = 0 \text{ at } y = 0, L$$

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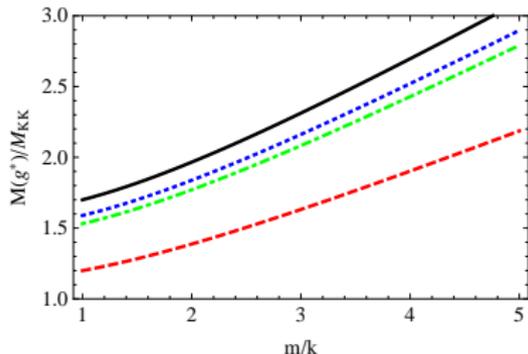
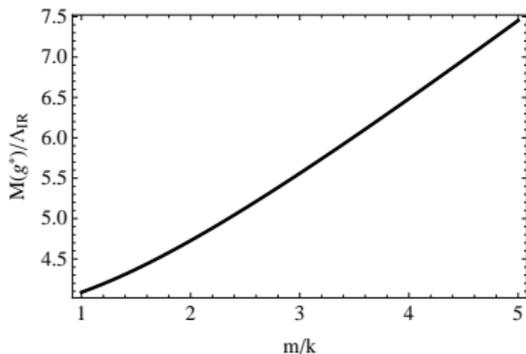
$$(\partial_y \pm 2k) B_{\mu\nu} = 0 \text{ at } y = 0, L$$

The Spectrum and Kaluza-Klein Functions

- Standard Kaluza-Klein Expansion:

$$B_{\mu\nu}(x, y) = \frac{1}{\sqrt{L}} \sum_{n=1}^{\infty} B_{\mu\nu}^{(n)}(x) f^{(n)}(y).$$

- Lightest states localised near $y = L$ (of course ...)
- Note mass \geq KK gluon, quark masses for $m \gtrsim 2.2k$

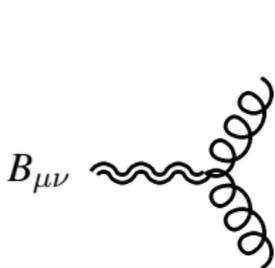


Coupling to the Gluon

- B - B - g coupling from kinetic term
- More interesting: B - g - g coupling

$$\mathcal{S}_{ggB} = \frac{g_5}{\sqrt{2}M_S^*} \int d^5x \sqrt{|G|} C^{abc} \left(F^{aLM} F^b_{L N} - \frac{1}{4} F^{aLK} F^b_{LK} G^{MN} \right) B^c_{MN}$$

- $C^{abc} = 2 \text{Tr}[t^a \{t^b, t^c\}]$



$B - g - g$	$B - g - g^{(1)}$	$B - g^{(1)} - g^{(1)}$
$1/\sqrt{kL}$	1	\sqrt{kL}

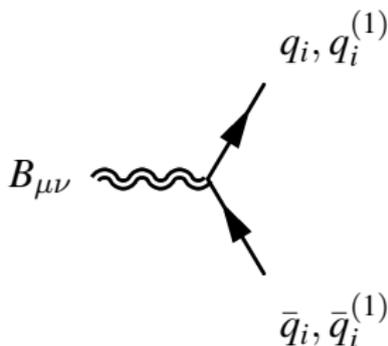
$g_{\sigma}, g_{\sigma}^{(1)}$

Coupling to the Quarks

- Also a $q\bar{q}B$ coupling, relevant for production & decay

$$\mathcal{S}_{q\bar{q}B} = -\frac{ig_5}{\sqrt{2}M_S^*} \int d^5x \sqrt{|G|} G^{LM} E_n^N \left(\bar{Q}_i \Gamma^n \tilde{B}_{LN} \mathcal{D}_M Q_i - h.c. \right).$$

- $\tilde{B}_{MN} \equiv t^a B_{MN}^a$

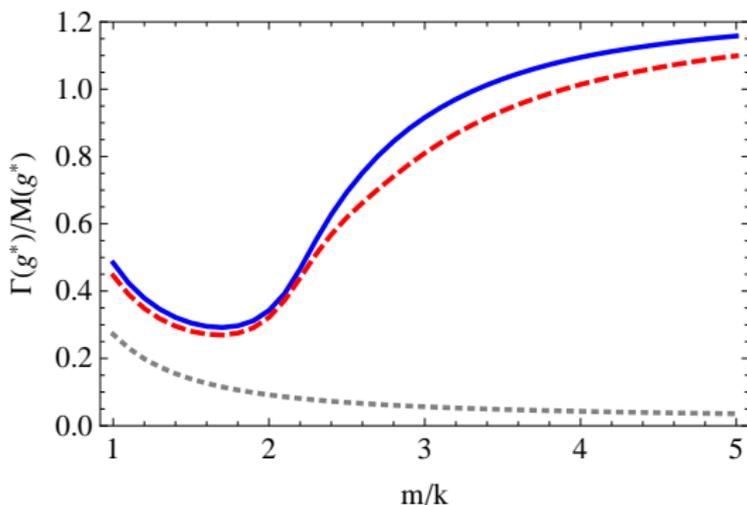


$$B - q - \bar{q} \quad \frac{\sqrt{kL}(1-2c)}{1-\exp[(2c-1)kL]}$$

$$B - q - \bar{q}^{(1)} \quad \sqrt{\frac{kL(1-2c)}{1-\exp[(2c-1)kL]}}$$

$$B - q^{(1)} - \bar{q}^{(1)} \quad \sqrt{kL}$$

Total Decay Width



- Note width \gtrsim mass for $m \gtrsim 2.2k$
- Assumed Regge gluon on-shell (to factorise Veneziano \mathcal{A})
- Restrict ourselves to m below this cut-off

Branching Fractions

Figure: Higgsed

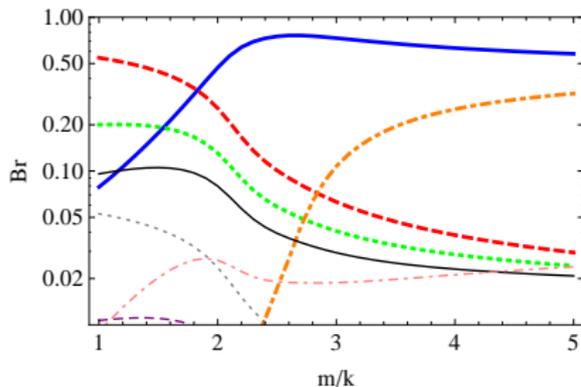
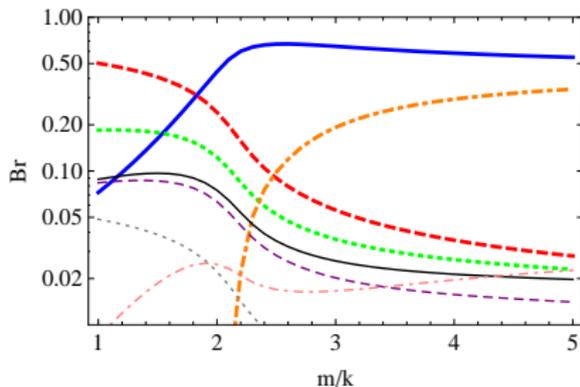


Figure: Higgsless

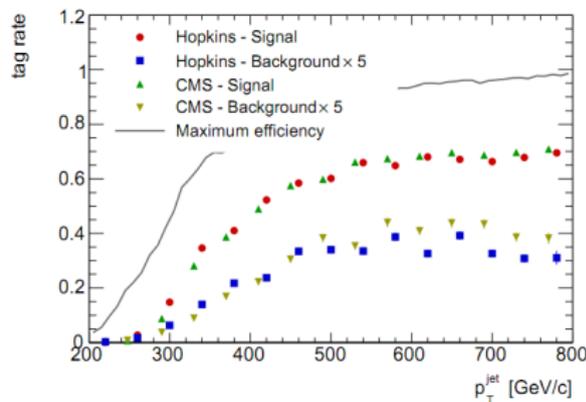


- Decay to SM ($t\bar{t}$) only dominates for $m \lesssim 1.5k$
- Decay to two KK gluons (one off-shell) dominant otherwise
- Decay chain $B \rightarrow g^{(1)}g^{(1)} \rightarrow t\bar{t}t\bar{t}$

Identifying Energetic Tops

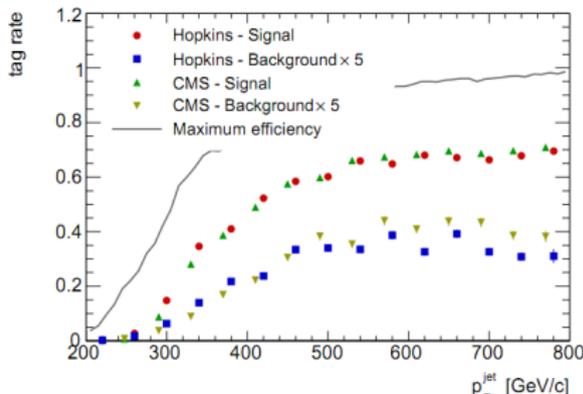
Top Tagging Algorithms

- Regge gluon mass $\gtrsim 1.5$ TeV
 - Tops typically have $E \gtrsim 400$ GeV, **highly boosted**
 - Decay products collimate into “**top jets**”
 - Need to distinguish top jets from ordinary QCD jets
-
- Many tools to do this, using jet substructure
 - Trade off between acceptance and purity
 - Use existing studies of tagging algorithms and apply to our model (BOOST 2010, 1012.5412)



Defining the Signal and Backgrounds

- Cannot* put Regge gluon into event generator
 - “Generate” signal by assuming:
 - Regge gluon produced approximately at rest;
 - Decays to two KK gluons approximately at rest;
 - KK gluons decay isotropically to tops
 - This gives top p_T distribution
-
- Background: QCD, n jets + $(4 - n)$ tops
 - Dominated by $jjjj$
 - Demand four tags ...
 - ... but high tagger eff.
 - Fix fake rate (no p_T dependence)



Signal Cross Sections: 7 TeV

Figure: Higgsed

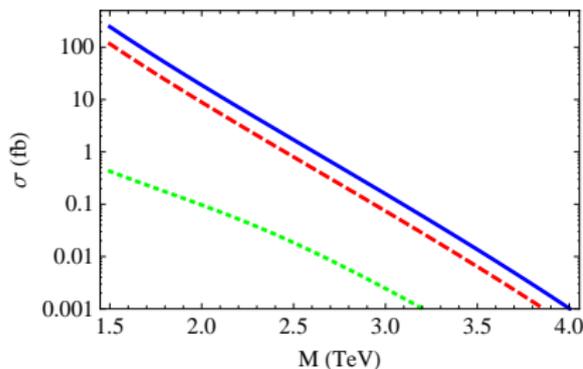
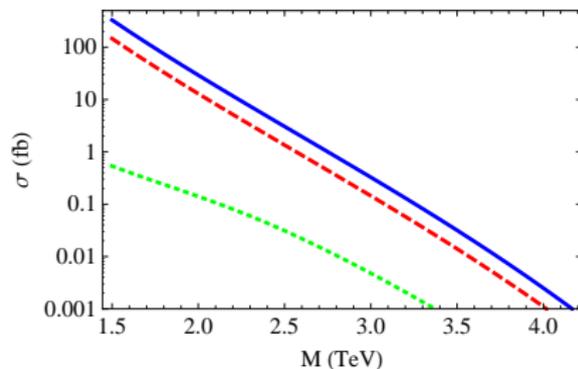


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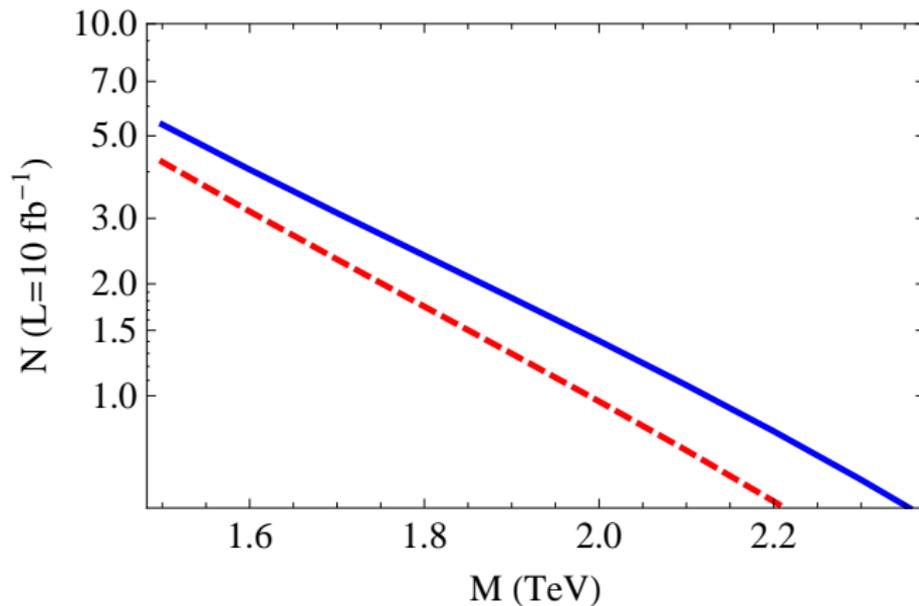


- Total cross section ~ 100 s of fb
- Cross section less than 1 fb after cuts

Prospects for Detection: 7 TeV

Number of Signal Events in 10 fb

- Negligible backgrounds ($\lesssim 0.1$ events)



Signal Cross Sections: 14 TeV

Figure: Higgsed

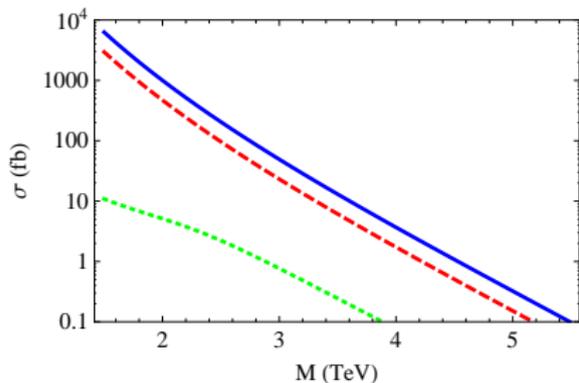
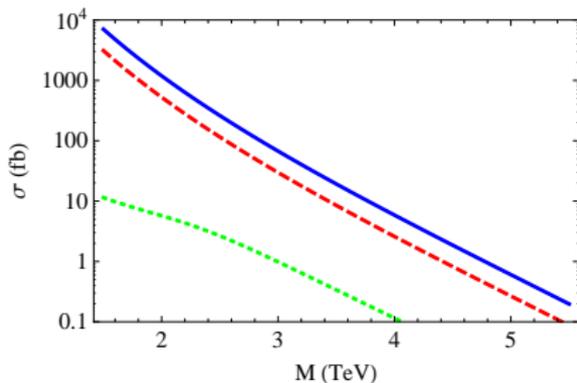


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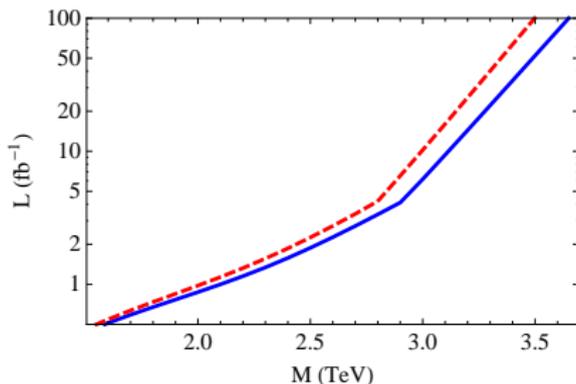


- Total cross section 1–10 pb
- Cross section 1–10 fb after cuts

Prospects for Detection: 14 TeV

Luminosity for Discovery

- Backgrounds ~ 0.24 fb



- For $M \lesssim 2.7$ TeV, limited by number of events
- Otherwise demand $S/\sqrt{B} \geq 5$
- In all region plotted, signal \geq background

Conclusions and Future Directions

- String Theory + Randall-Sundrum suggests **TeV-scale, high-spin** partners of SM
- Regge gluon decays to **four highly boosted top quarks**
- Difficult to see at 7 TeV LHC; **detectable** at **14 TeV LHC**
- Obvious next step: Implement model in **event generators**